

# FIRST PRINCIPLES MODELING OF NOVEL FUNCTIONAL MATERIALS FOR FUEL CELL APPLICATIONS

*E. A. Kotomin*

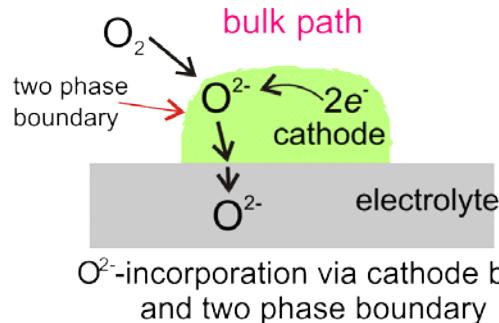
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# General problem

Improvement of SOFC and permeation membrane performance requires better understanding of oxygen reduction reaction

cathode reaction:  $O_2(g) + 4e^- \rightarrow 2O^{2-}$

Study and control of possible reaction pathways of oxygen reduction and incorporation reaction



Exciting and challenging multidisciplinary field:  
-Electrochemistry and materials chemistry,  
- surface science of advanced oxides,  
-, chemical kinetics,  
-large-scale computer simulations

# Development of new materials

- **Large scale computer simulations** of materials in close collaboration with state-of-the art experiments [Max Planck Institute, Stuttgart]:  
**Combinatorial approach:** J.Serra, V.B.Vert, ChemSusChem 2, 957 (2009) is time-consuming  
**Limitations** of experiments:  
Discrimination of processes (O vacancies migration) in the bulk and on surfaces,  
A role of different dopants and impurities  
Identification of adsorbates at low coverages

## **Goals of theory:**

Atomistic/mechanistic details of oxygen reduction (ORR) at SOFC cathode surface;

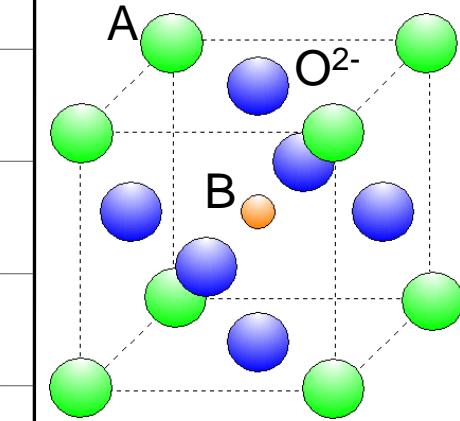
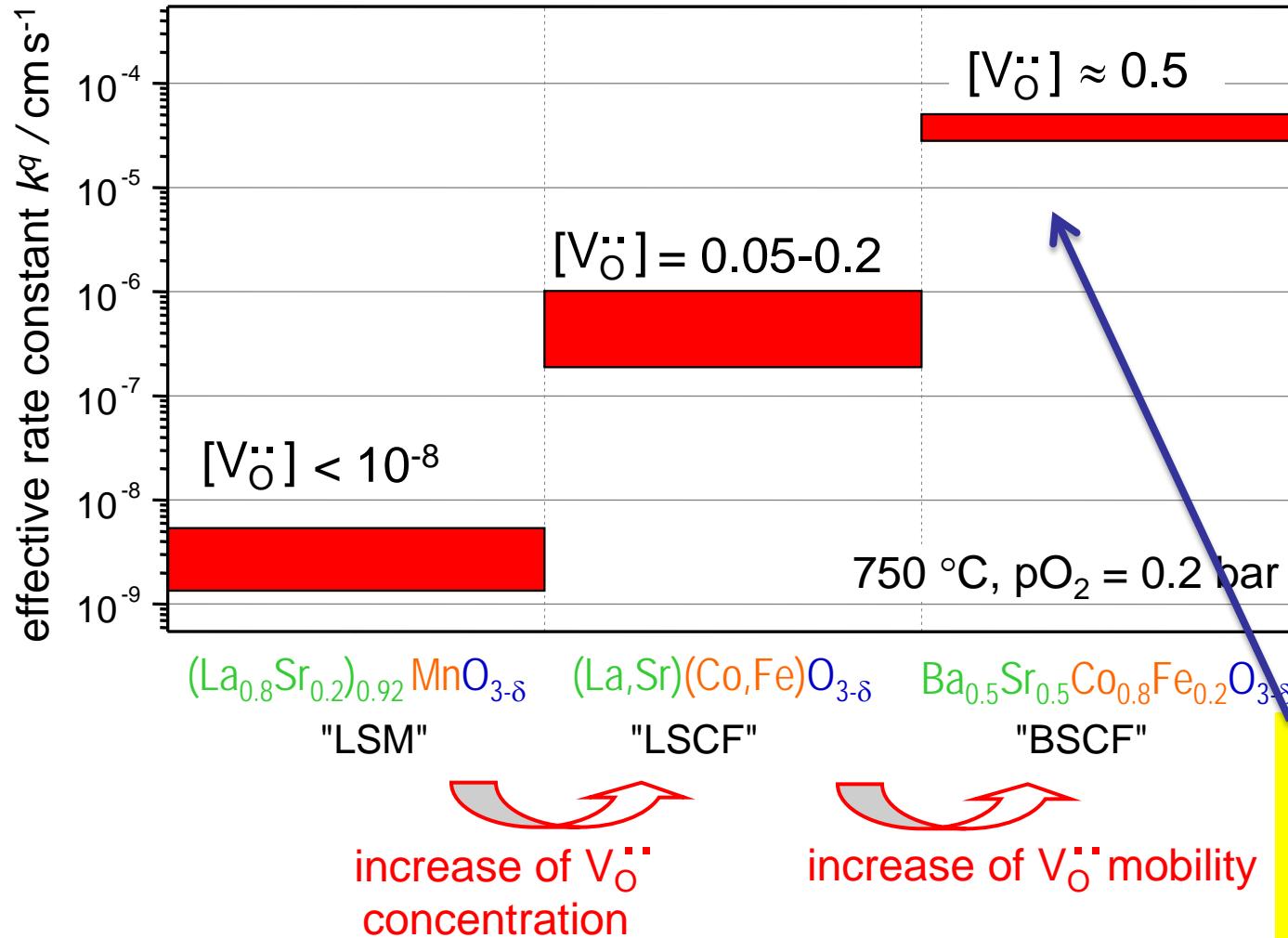
**-- O vacancy formation/migration on the surface/bulk; optimisation of cathode chemical composition**

Challenge: what are the rate-determining reaction stages in oxygen reduction reaction

# Joint experimental- theoretical study on BSCF-LSCF

- R.Catlow (ed.) Computational Approaches to Energy Materials, Wiley, 2013, Chapter 6.
- M. Kuklja et al, PCCP (Perspective) 15, 5443 (2013)
- R. Merkle et al, JECS 159, B 212 (2012)
- Yu. Mastrikov et al, PCCP 15, 911 (2013)
- D. Fuks et al, J. Mater.Chem.A, 1, 14320 (2013)

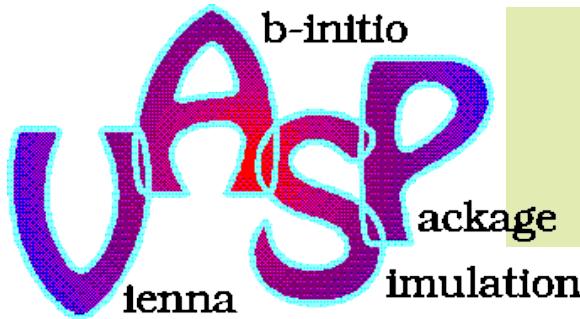
# SOCF perovskites cathode materials comparison



Both migration and formation energies are important!!

F. S. Baumann et al., *J. Electrochem. Soc.* 154 (2007) B931; J. Fleig et al., *Fuel Cells* 8 (2008) 330

L. Wang et al., *J. Electrochem. Soc.* 157 (2010) B1802



# Methods: 1. Solid state physics

## Density Functional Theory Plane Wave basis set

**Generalised Gradient Approximation (Hubbard U)**

**Perdew Wang 91 exchange-correlation functional**

**Projector Augmented Wave** method

**Davidson** algorithm for electronic optimization

**Conjugate Gradient** method for structure relaxation

**Nudged Elastic Bands** for energy barriers estimation

**Bader charge analysis** (**Prof. G. Henkelman** and co-workers, *Universiy of Texas*)

**Spin-polarized calculations**

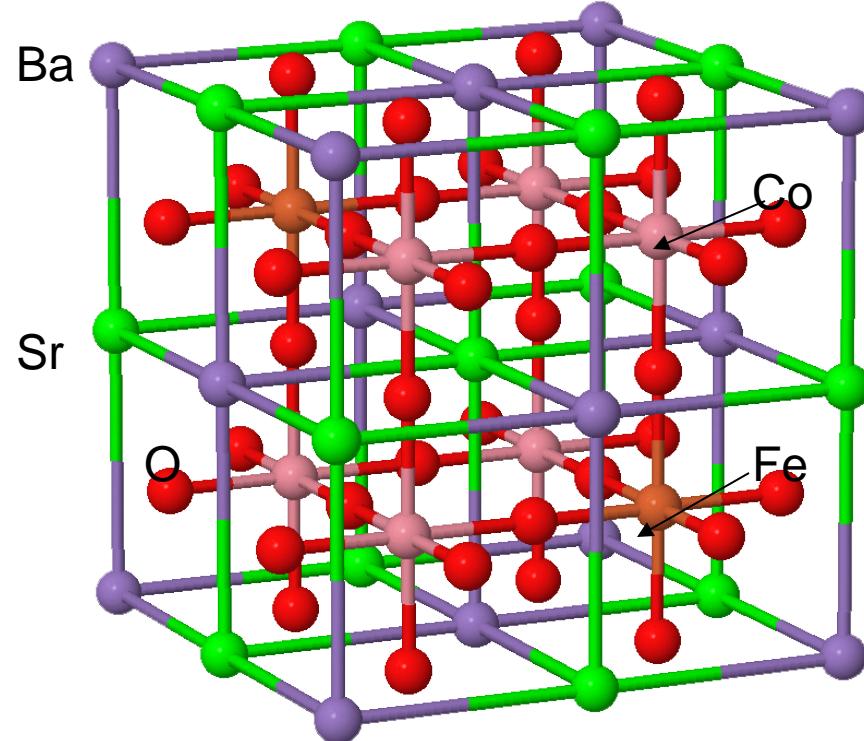
- **2. Quantum chemical approach**
- **CRYSTAL** code with LCAO basis set
- (re-optimised Comp Mat Sci. 29, 165 (2004)

For light atoms (O), all-electron basis set (BS) for heavy atoms (Sr, Pb,Ti and Zr), the **small-core Hay-Wadt pseudopotentials**

- **Hybrid HF-DFT functionals**
- hybrid functionals work very good!  
The gap 3.63 eV(indirect); 3.95 eV(direct): 10% error
- $a_0=3.91 \text{ \AA}$  ( + 0.5% error)
- **Supercell model** (up to 320 atoms:  $4 \times 4 \times 4$  extended UC)

# The most efficient SOFC material: $\text{Ba}_{(0.5)}\text{Sr}_{(0.5)}\text{Co}_{(0.75)}\text{Fe}_{(0.25)}\text{O}_{3-\delta}$

- 



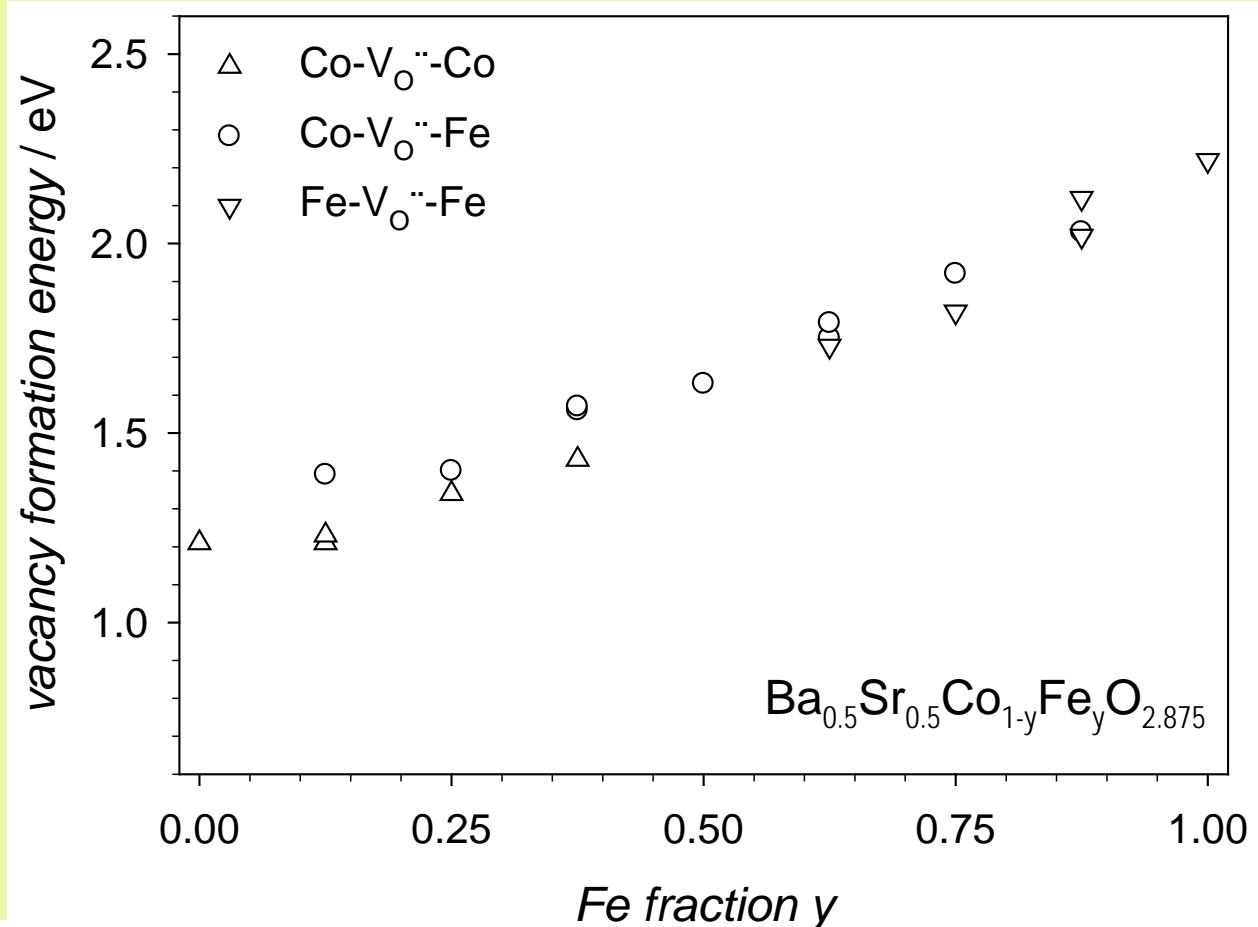
**Bulk and defect properties**

40 atom supercells (4% of oxygen vacancies) and 320 atoms (0.7%)

**Mastrikov et al, En. Env. Sci. 3, 1544 (2010).**

# Role of chemical composition: defect formation energies [Kotomin et al, Sol. St. Ionics, 188, 1 (2011)]

BSCF



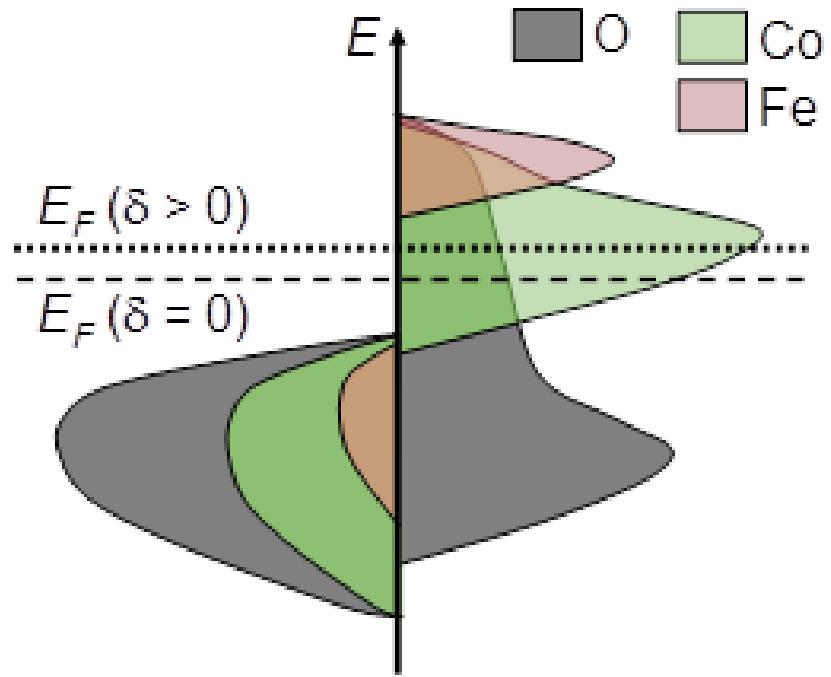
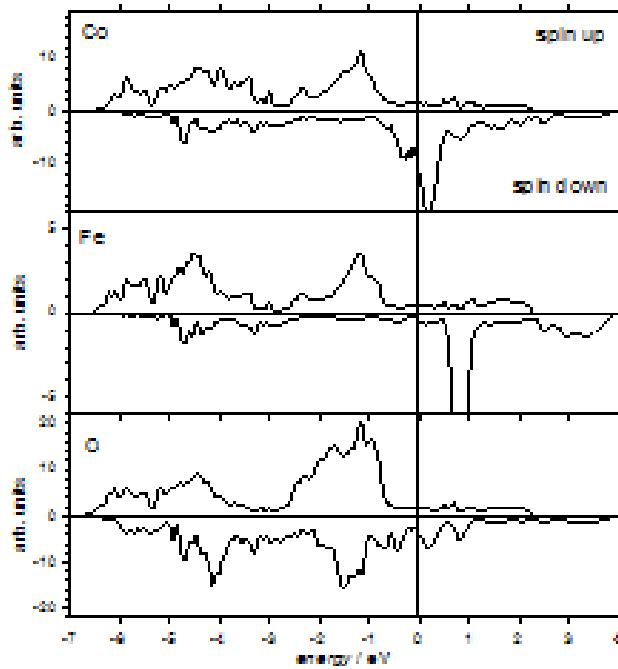
# Composition trend

- Vo formation energy increases considerably with Fe concentration ( $1.2 \rightarrow 2$  eV) [with respect to the free O atoms:  $\frac{1}{2} O_2$  ],  
in agreement with expt observation of defect concentration increase BSF  $\rightarrow$  BSCF (Gauckler et al, PCCP 11, 3090 (2009))

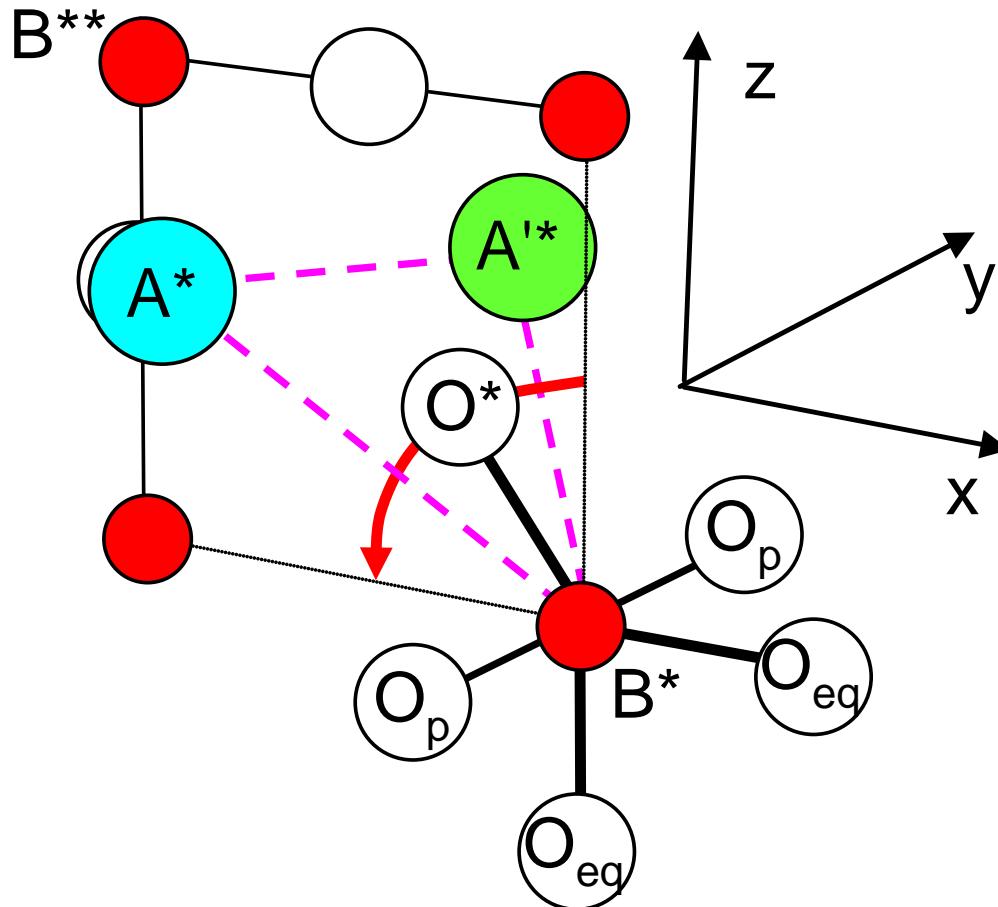
BSCF formation energy much smaller than in LSM (2.7 eV) and STO (5.9 eV)

# Explanation from DOS analysis

R. Merkle et al, JECS 159, B 219 (2012)

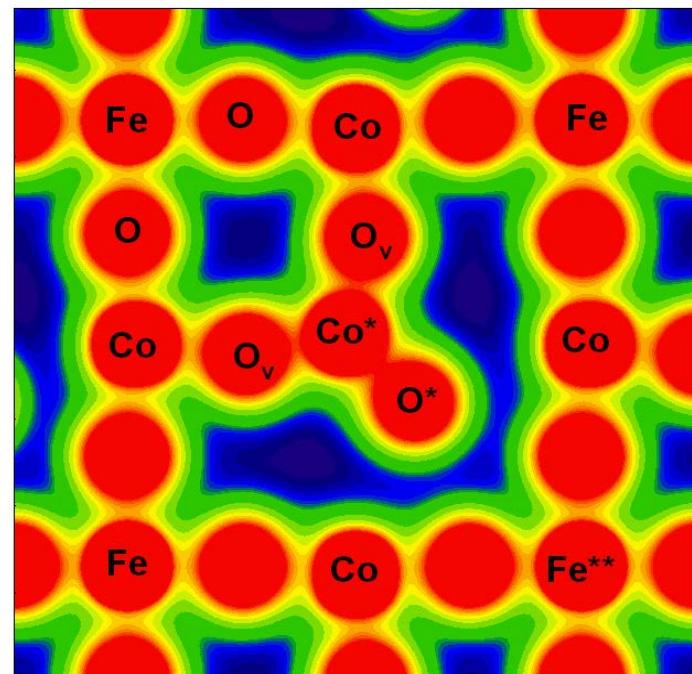
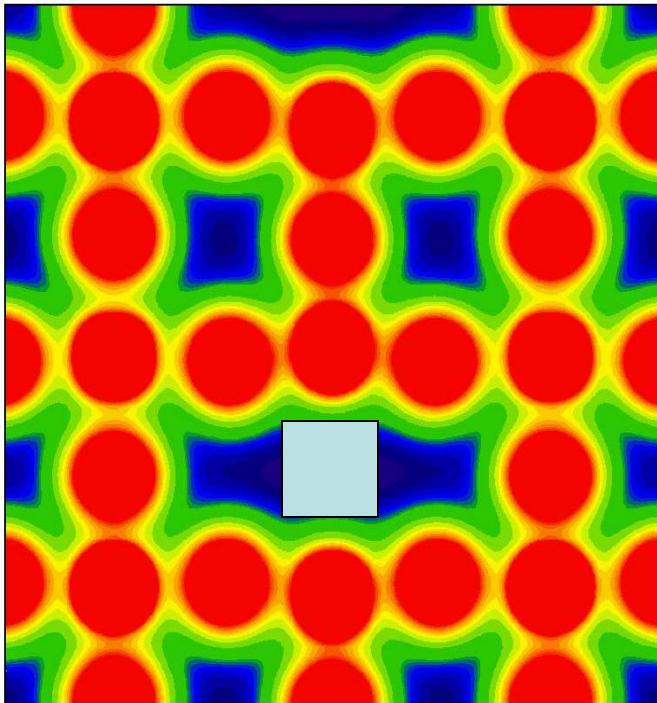


# Transition state of O migration



**Key factors:**  
-Lattice expansion  
-Charge transfer

# BSCF(001) electron density maps

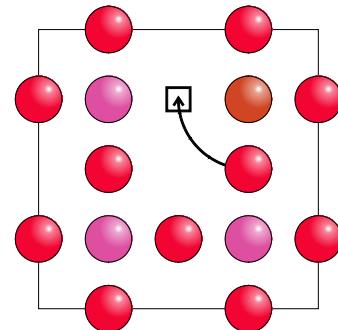


**a) Equilibrium state for oxygen vacancy; b) transition state**

Merkle et al, JECS 159, B219 (2012)

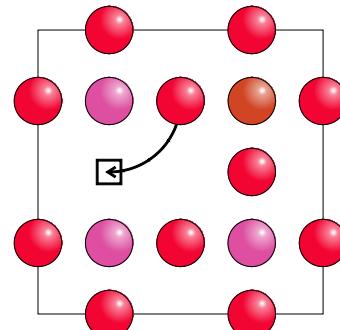
# Vacancy migration energy, $\text{Fe}_{0.25}$

Co-Vo-Fe



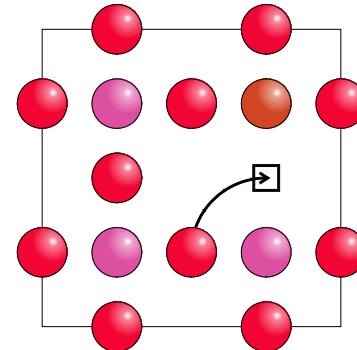
0.46 eV

Co-Vo-Co



0.52 eV

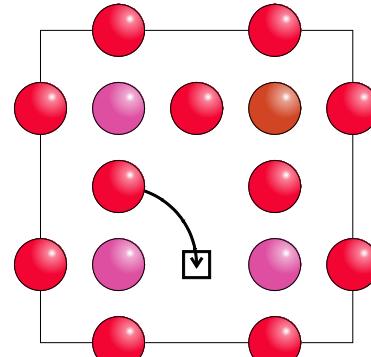
0.46 eV



Co-Vo-Fe

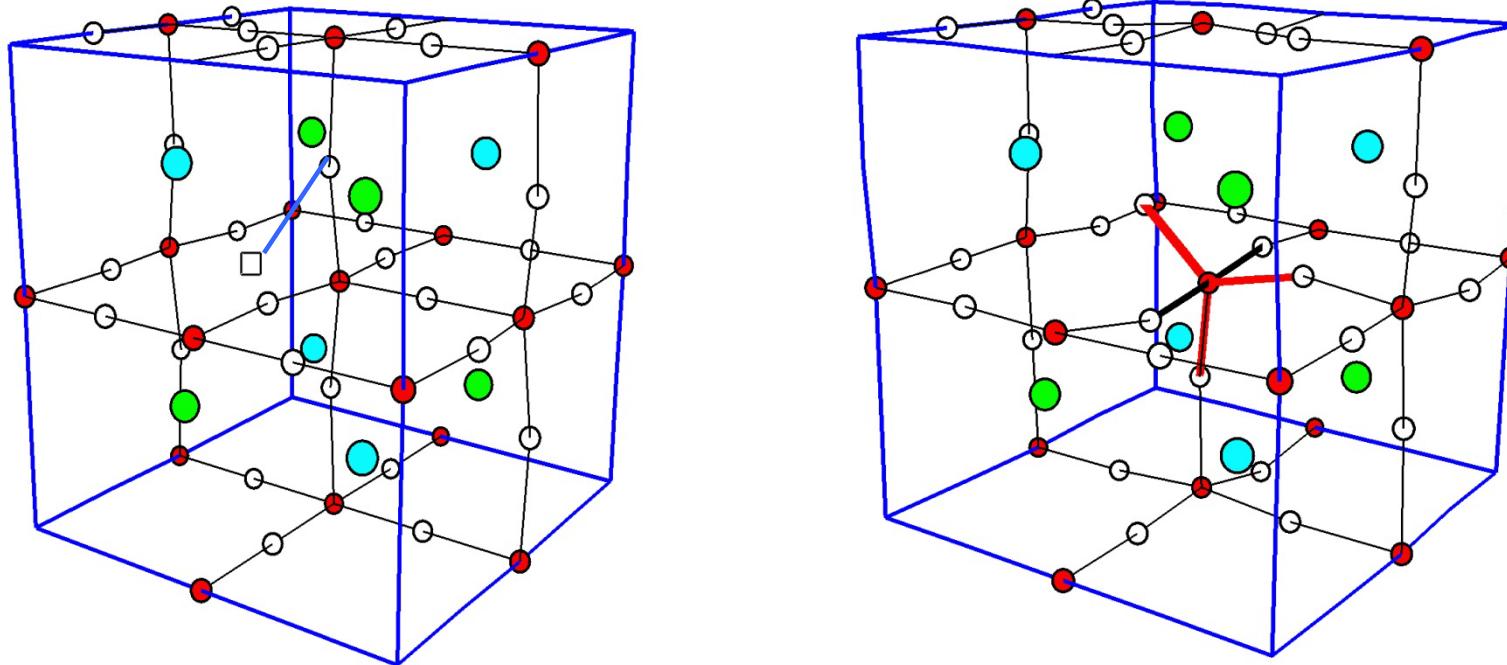


Co-Vo-Co  
0.42 eV



For comparison: LMO 0.9 eV

# Vacancy migration in BSC: ground and transition states

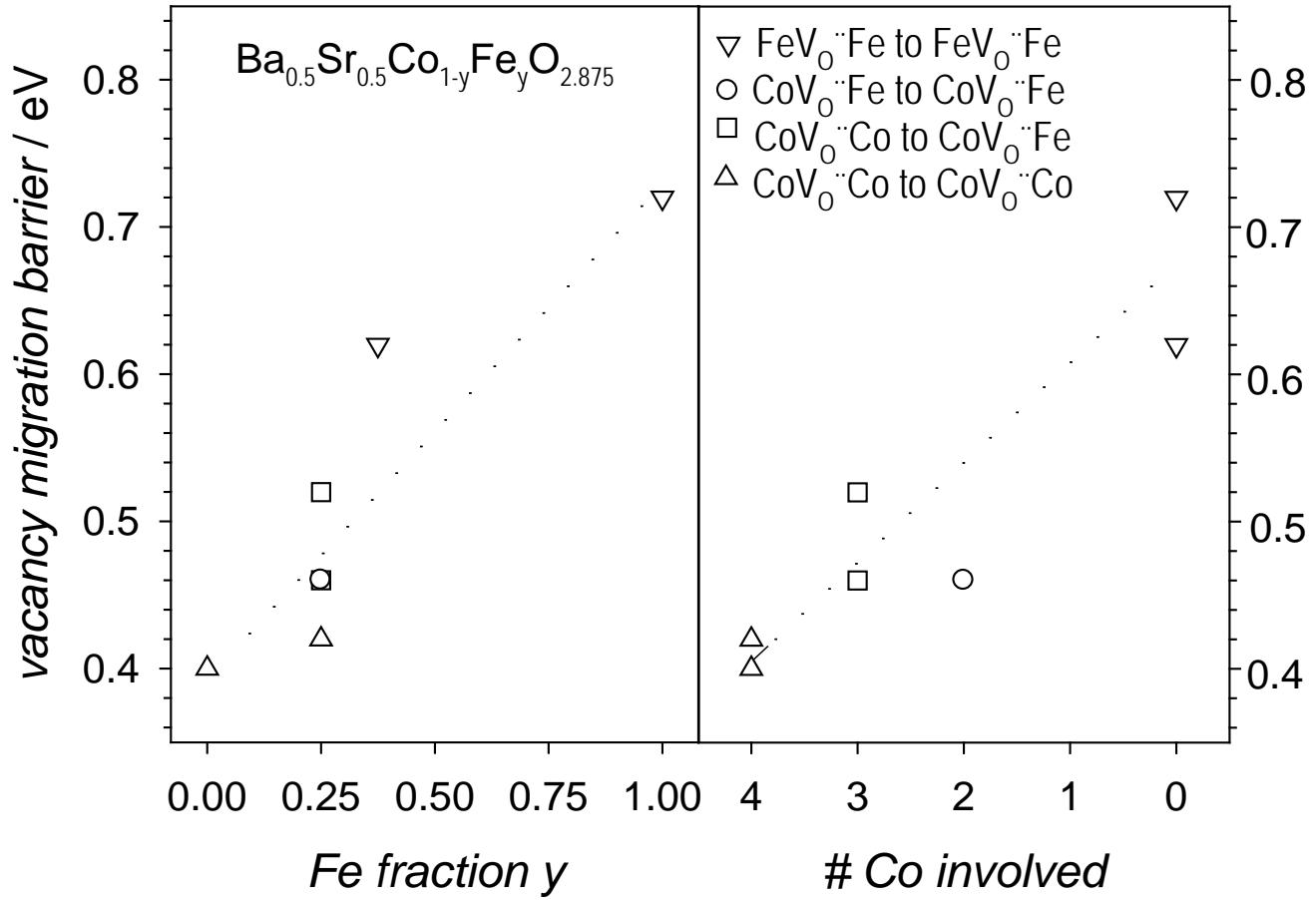


Lattice distortion areas is 6-8 Å around the jumping O<sup>\*</sup> ion

# Vacancy migration energies

Kotomin, Sol.St.Ionics, 188, 1 (2011); Merkle et al, JECS 159, B219 (2012)]

BSCF

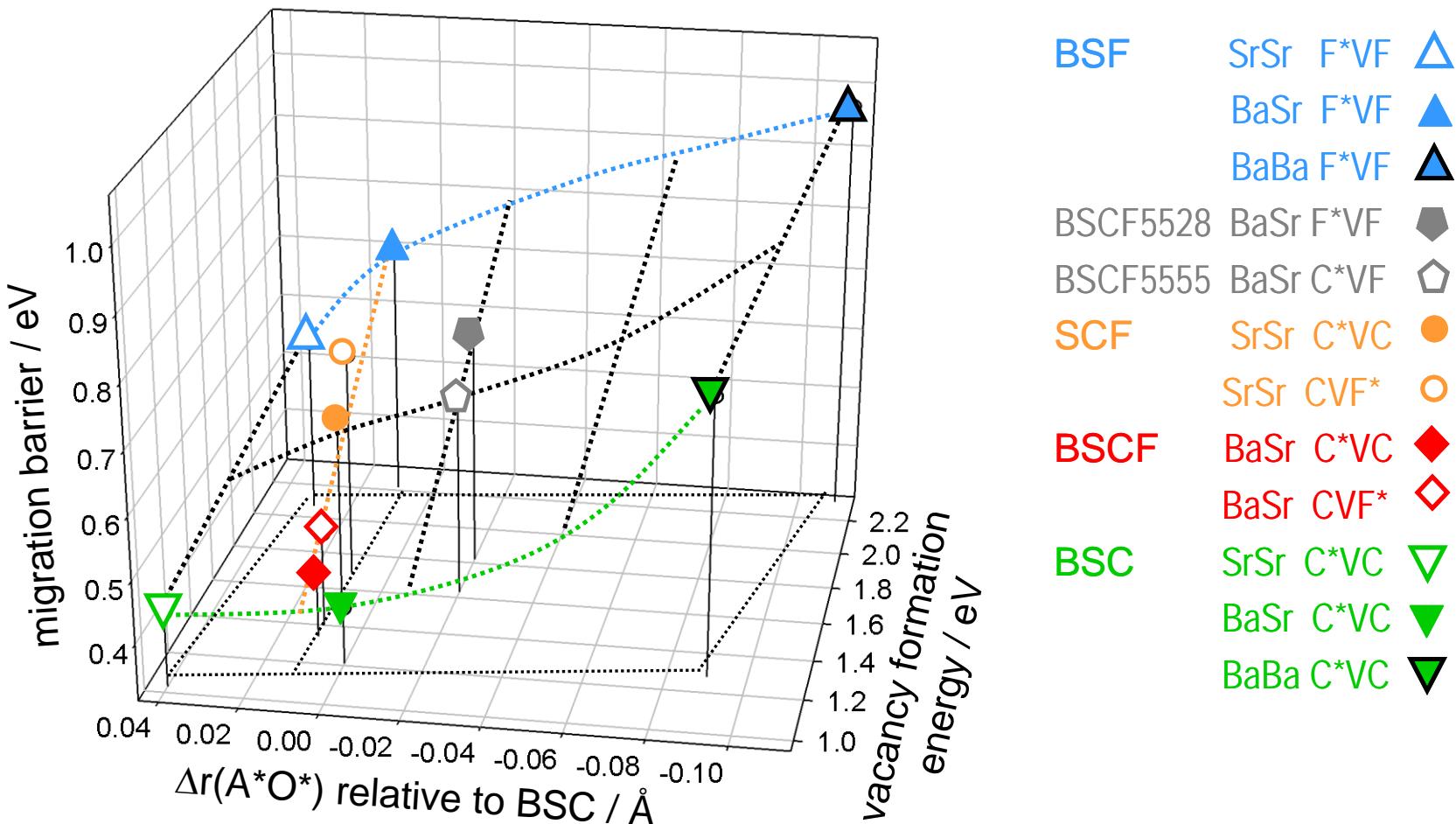


# Trend

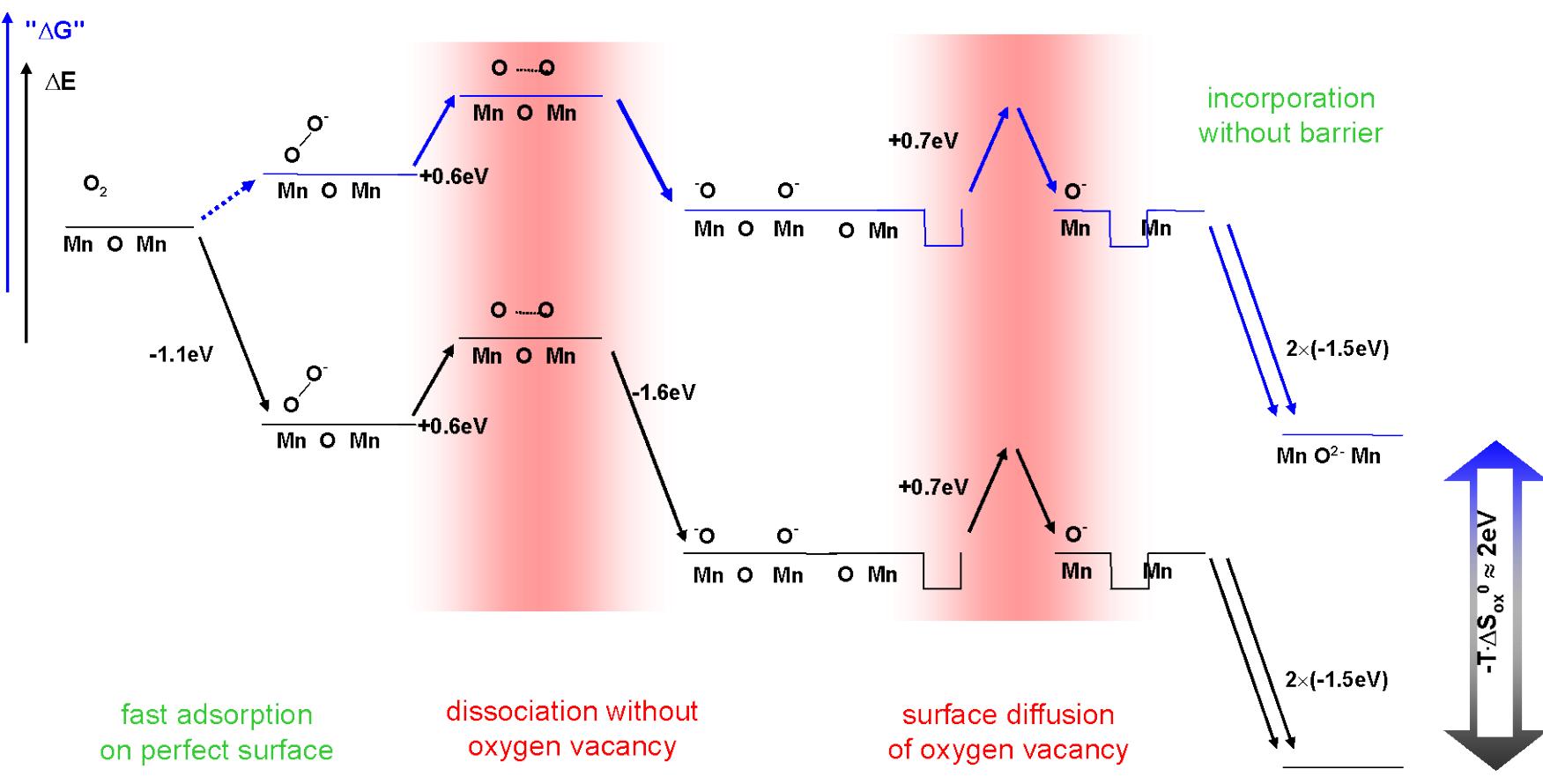
- Migration energies much smaller in BSCF (~0.5 eV) than in LMO, LFO,LCO, STO (0.8-0.9 eV)
- Energy increase with Fe concentration
- What are the main factors behind?

**Migration energy** depends on both the saddle point geometry and electronic structure (vacancy formation energy)

Merkle et al, JECS 159 (2012) B 219; Kotomin, SSI 188 (2011) 1

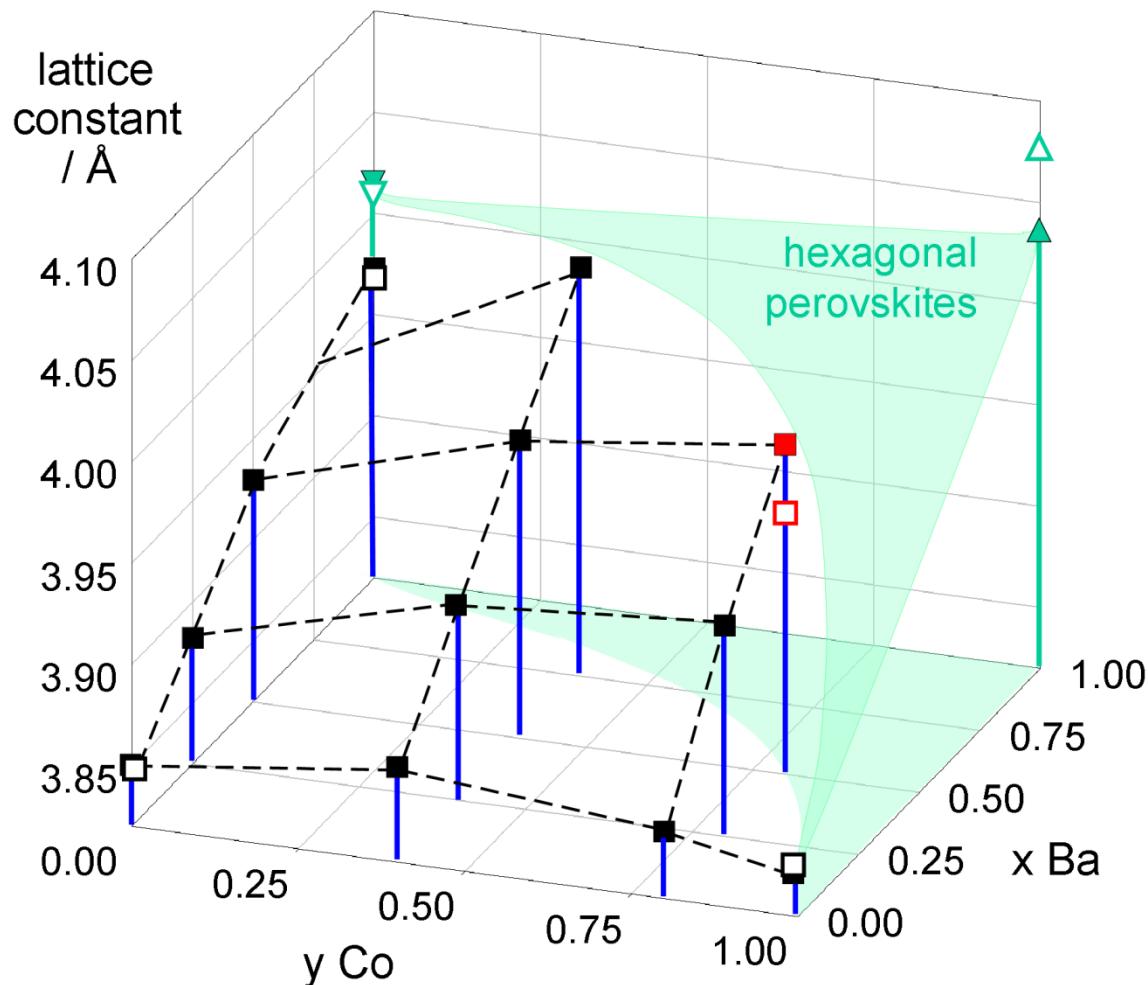


Our goal is modelling of all steps of the ORR in order to find limiting one **Entropy effects** important under realistic operational conditions: LSM



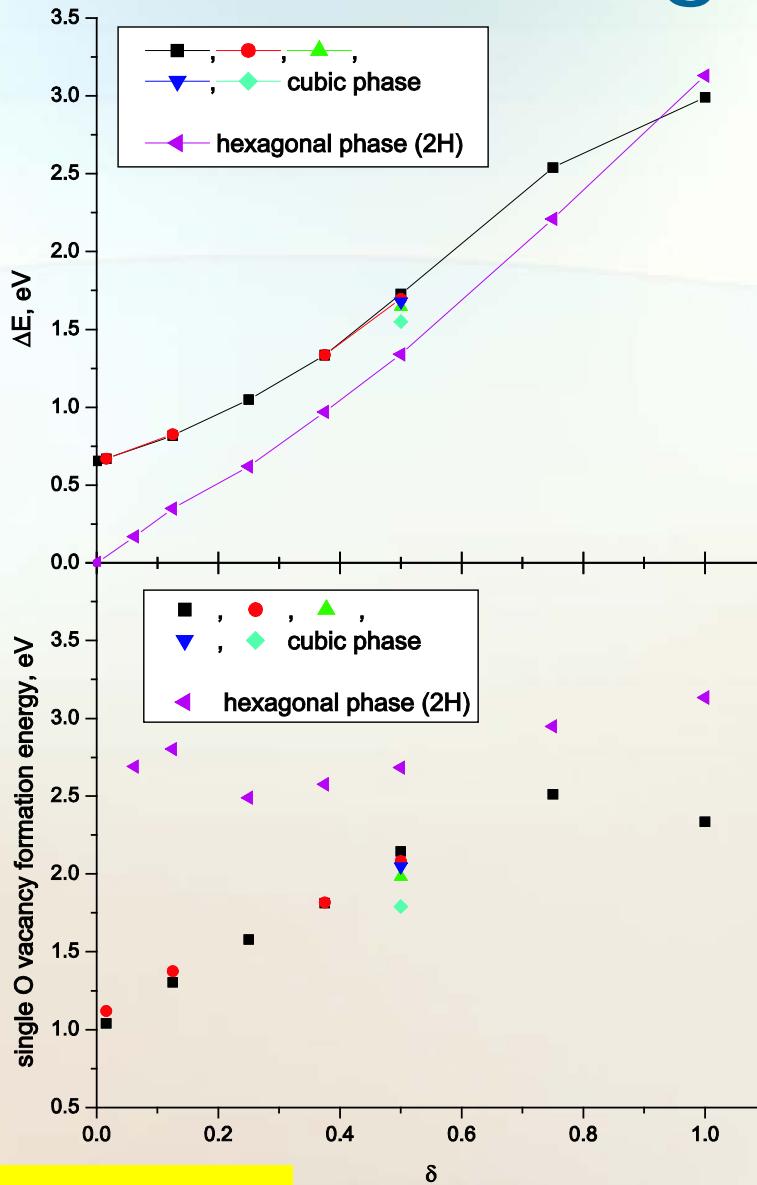
Mastrikov et al, J. Phys. Chem. C 114, 3017 (2010); Wang J. Mat. Res. 27, 2012

# Cubic vs hexagonal?



**Chemical expansion coefficient is close to expt value**

# BSCF: cubic vs hexagonal?



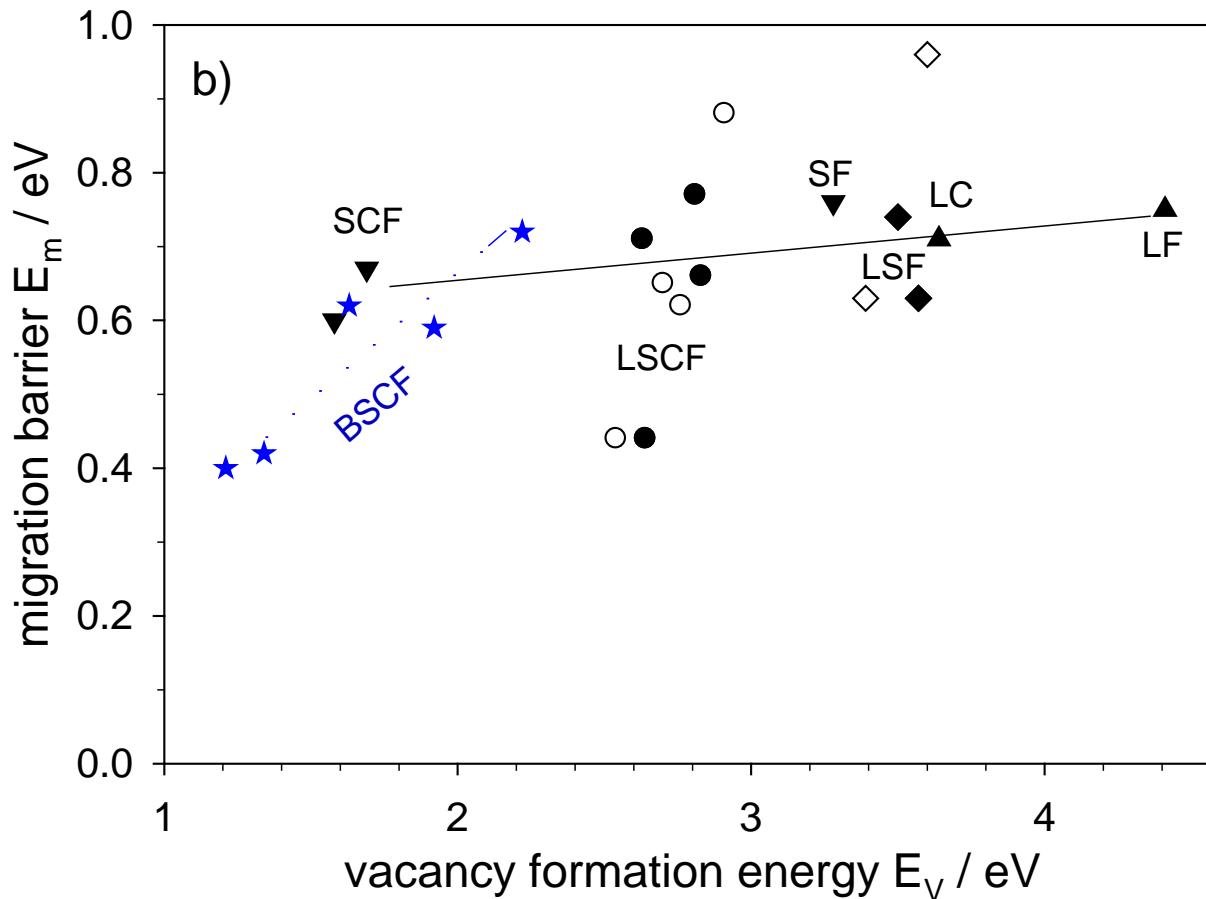
# CONCLUSIONS

- First-principles computer modeling could be useful tool for understanding „composition-property“ relation in complex perovskite solid solutions (**where simple models fail**)
- especially at surfaces/interfaces (defect formation energies and mobilities, charge distribution, etc.) and transition states of processes
- Intuitive conclusions are **not** always correct, e.g. defect formation energies at surfaces and in bulk
- Structural stability aspects!! **Kuklja et al, J Phys Chem C 116, 18605 (2012)**

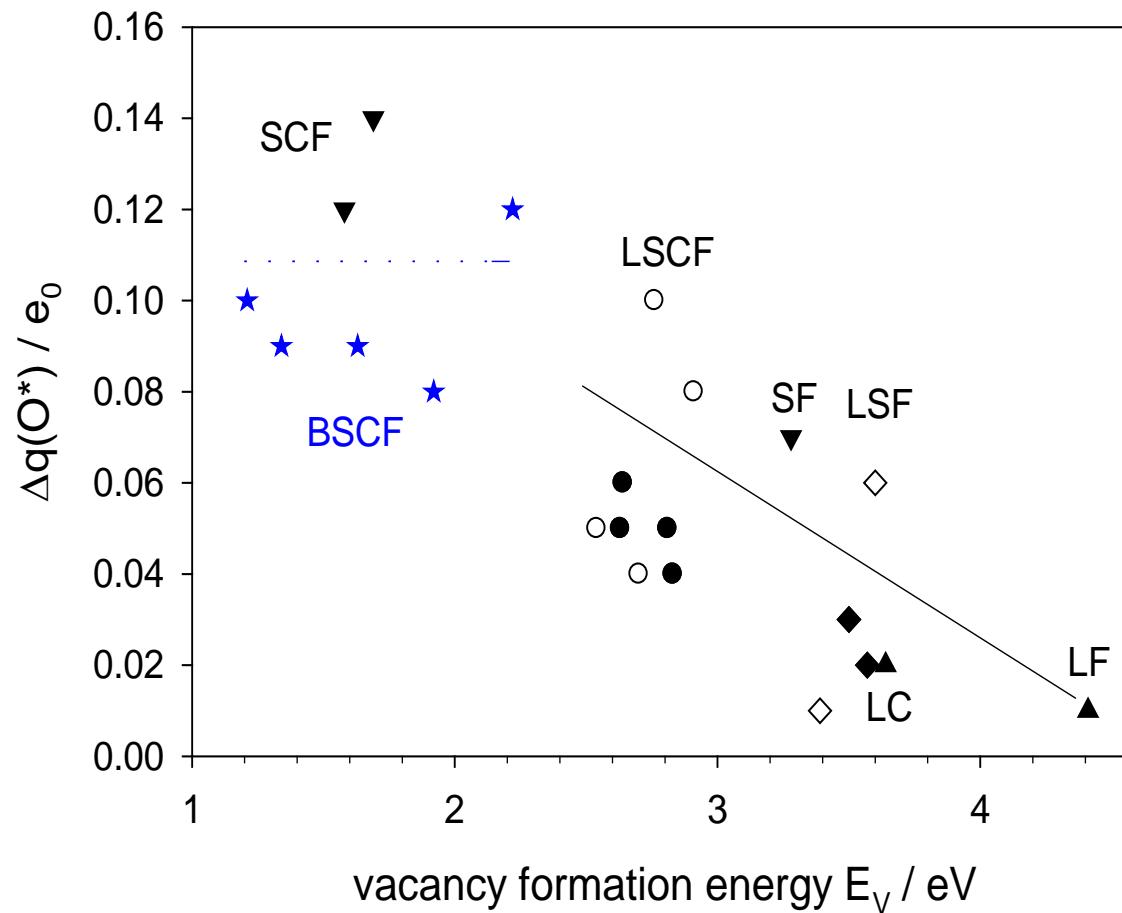
- Many thanks due to:
- R.Evarestov (St Petersburg University)
- D.Gryaznov, Yu.Mastrikov (University of Latvia)
- M. Kuklja (Maryland University, USA)
- D. Fuks (Ben Gurion University, Israel)
- J.Maier, R. Merkle (Max Planck Institute, Stuttgart)

# LSCF: almost no correlation!

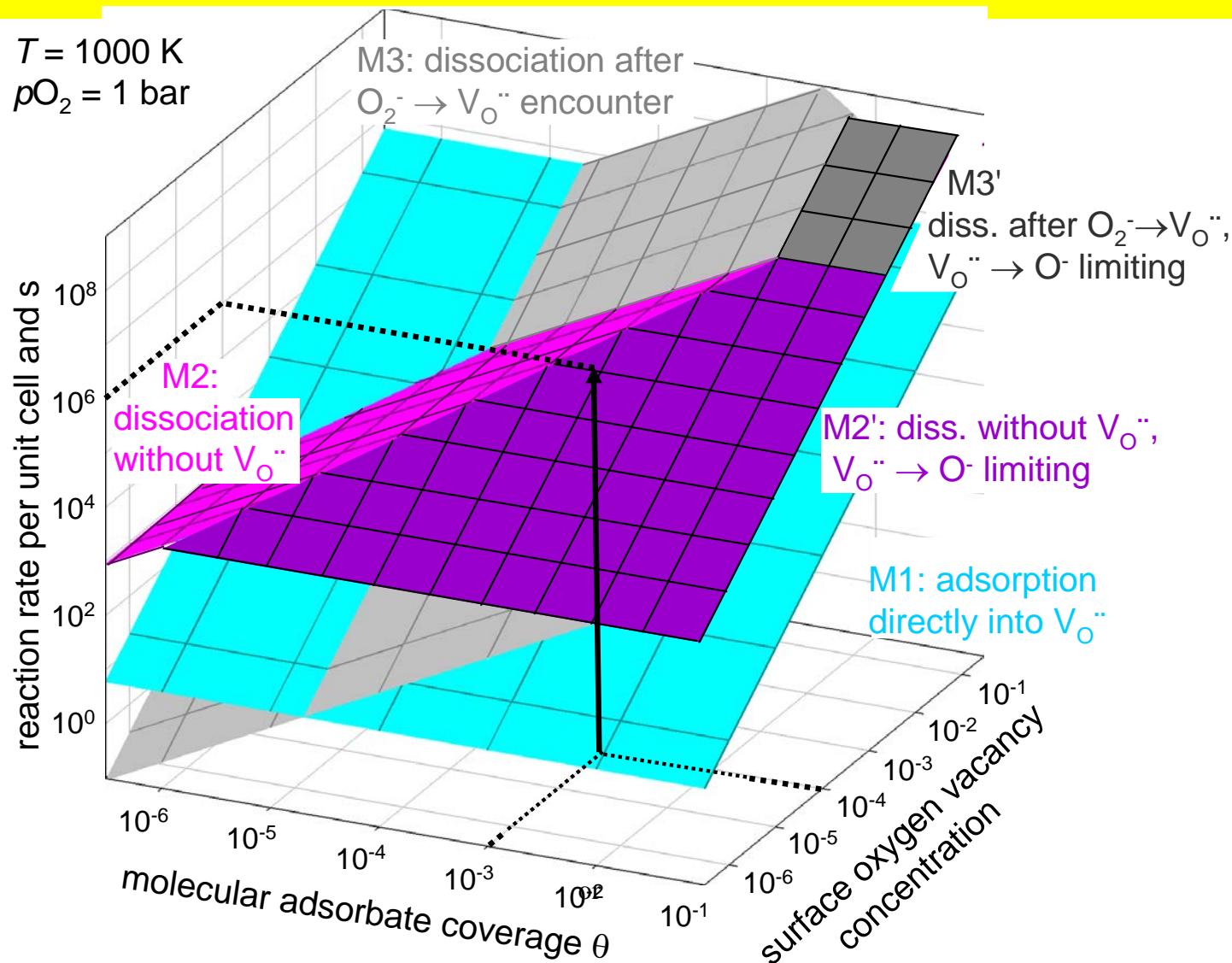
*Mastrikov et al, PCCP 15, 911 (2013)*



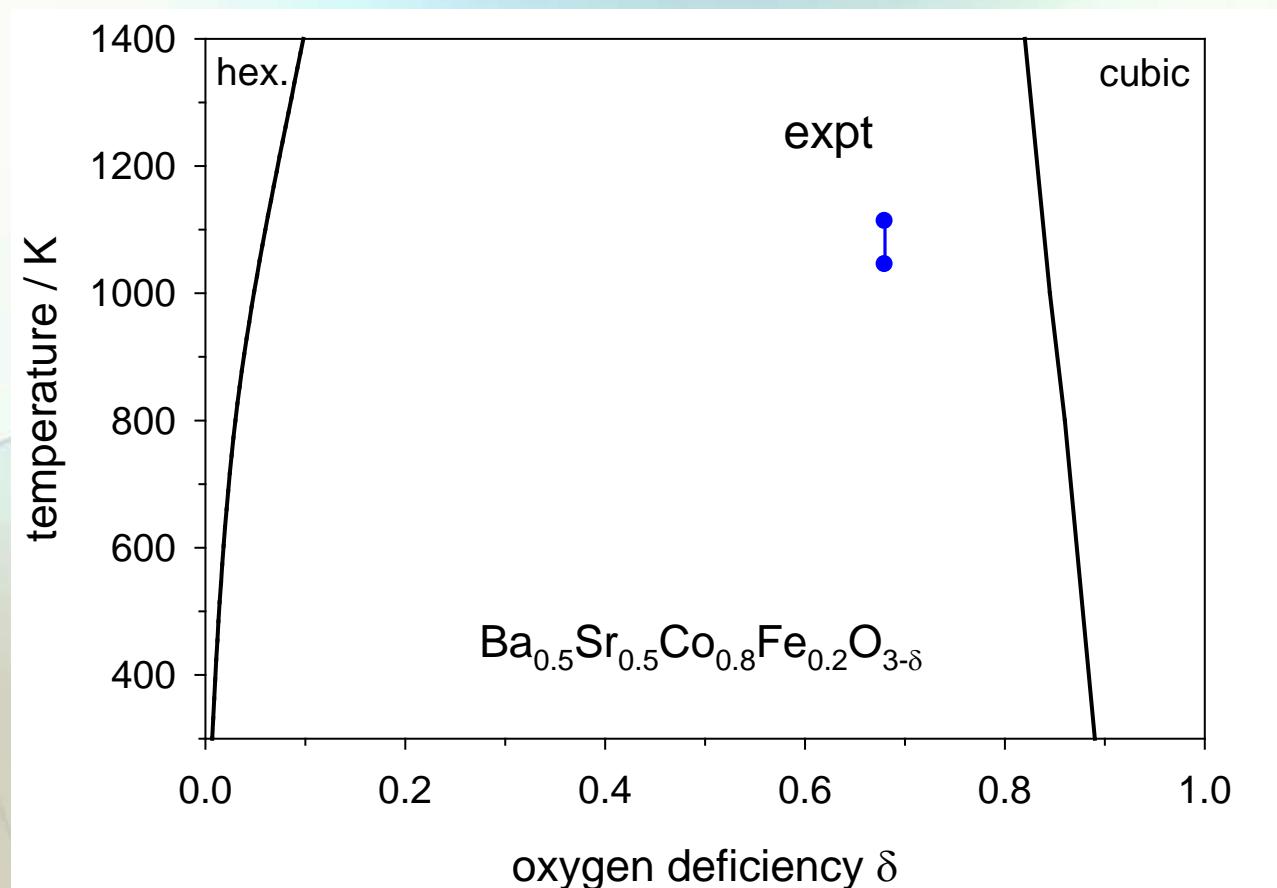
# ...and negligible charge transfer



# Variation of oxygen exchange rates for MnO<sub>2</sub>- termination



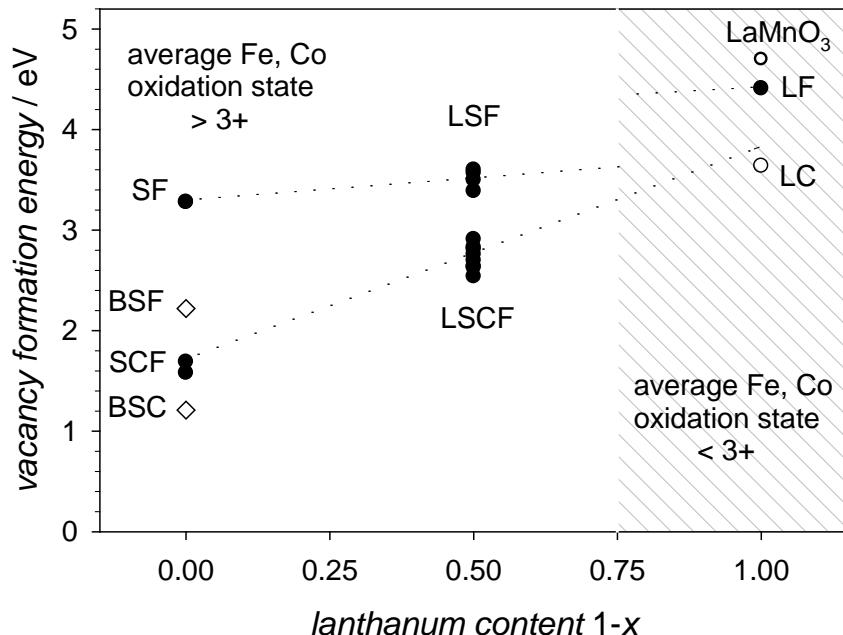
# Phase diagram (ab initio TD)



Phase diagram of hexagonal/cubic BSCF 5582  
from thermodynamic modeling

# Diffusion in LSCF: contrast to BSCF

Mastrikov et al, PCCP 15, 911 (2013)



Oxygen vacancy formation energy  $E_v$  as a function of lanthanum content  $1-x$  in  $\text{La}_{1-x}\text{Sr}_x\text{Co}_{0.8}\text{Fe}_{0.2}\text{O}_{2.875}$  (circles), several data for a given cation composition refer to different cation configurations around the vacancy.  
For comparison,  $E_v$  of BSF, BSC22,24 and orthorhombic  $\text{LaMnO}_3$  are included (open symbols).

# A role of Sr doping in Vo formation energy in $\text{La}_{(1-x)}\text{Sr}_x\text{FeO}_{3-\text{d}}$

- Two limiting cases:  $\text{LaFeO}_3$  (oxidation state 3) and  $\text{SrFeO}_3$  (oxidation state 4)
- each Sr (+2) atom brings a hole:  $\text{Fe} \rightarrow +4$
- Each oxygen vacancy Vo kills 2 holes:  $\text{Fe}(+3)$  or even  $\text{Fe}^{2+}$
- The Fe oxidation state is strongly affecting Vo formation energy (nonstoichiometry)
- The control parameter:  $d/2$  vs  $x$

# What does *ab initio* mean?

- Two global approaches: HF and DFT
- DFT: exchange-correlation functionals →
- LDA-type (only density)
- GGA (also density gradients)
- GGA+U (Hubbard U – on-site correlations)
- HF-DFT hybrids: semi-empirical or not

# Example: calculated band gap for defect-free ortho-LaFeO<sub>3</sub>

• Expt	2.1 eV
• LDA	metal
• LDA+U	2.3 eV
• GGA	0.75 eV
• GGA+U	2.53 eV
• HSE (hybrid)	3.6 eV

PS. LSF is a semiconductor up to 90% Sr.

## THE CALCULATED Vo FREE FORMATION ENTHALPY IN $\text{La}_{1-x}\text{Sr}_x\text{FeO}_{3-\delta}$

GGA calcs				
X, %	$\delta$ , %	$\Delta H$	Oxidation state Fe	expt
0 (LF)	12.5	4.26 (GGA)	2.75	5.0
50.0	12.5	3.5 (GGA)	3.25	0.99
100 (SF)	50	3.28 (GGA)	4.0	0.7

Mastrikov, PCCP 2013

## THE CALCULATED Vo FREE FORMATION ENTHALPY IN $\text{La}_{1-x}\text{Sr}_x\text{FeO}_{3-\delta}$

GGA+U, 900 K

X, %	$\delta$ , %	$\Delta H$ (900 K)	Oxidation state	expt
0 (LF)	12.5	3.99 (4.41)	2.75	5.0
25	12.5	0.69± 0.17 (1.1)	3.00	1.2
50	12.5	0.01± 0.28 (0.41)	3.25	0.99

Carter, Chem Mater 2013

## THE CALCULATED Vo FREE FORMATION ENTHALPY IN $\text{La}_{1-x}\text{Sr}_x\text{FeO}_{3-\delta}$

Hybrid PBE0 calculations, 1200 K

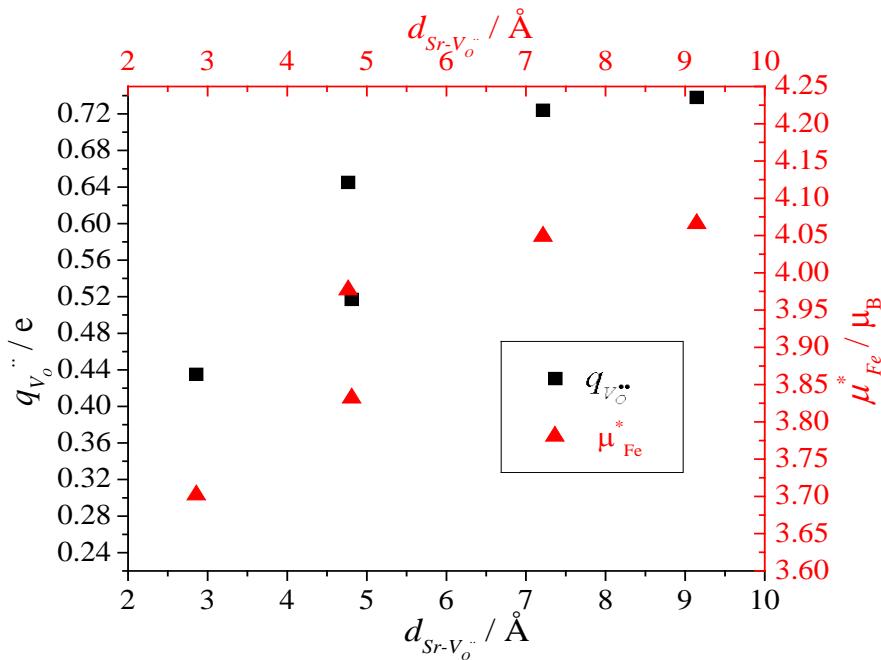
X, %	$\delta$ , %	$\Delta H$ (1200 K)	Oxidation state	expt
0 (LF)	12.5	4.26 (GGA) 3.99 (GGA+U)	2.75	5.0
12.5	12.5	2.2	2.875	3.0
12.5	6.25	0.89	3.00	1.2
25	12.5	0.69(GGA+U)		
50.0	12.5	0.15	3.25	0.99
		3.5 (GGA)		
		-0.01(GGA+U)		
100 (SF)	50	3.28 (GGA)	4.0	0.7

GGA- Mastrikov, PCCP 2013; GGA+U – Carter, Chem Mater 2013

Hybrid calculations give the best agreement with expt but...

## DISPERSION OF FORMATION ENERGIES IS QUITE LARGE:

6 types of Vo vacancies in 12.5% Sr  
Formation energies are ranged 0.68-1.09 eV



4 types of Vo for 50% Sr, energy are ranged 0.04-0.27 eV !!  
**Problem of averaging : kinetic MC**

## GENERAL CONSLUSIONS

1. Neither „*ab initio*“ method is perfect....
2. ... but hybrid functional are more reliable
3. Choice of a realistic model is non-trivial:  
inhomogeneous defect-dopant distributions,  
soft modes/unharmonicity in perovskites  
and phase transformations
4. Charged defects, especially in thin films is  
another challenge.

## Transition state complexity:

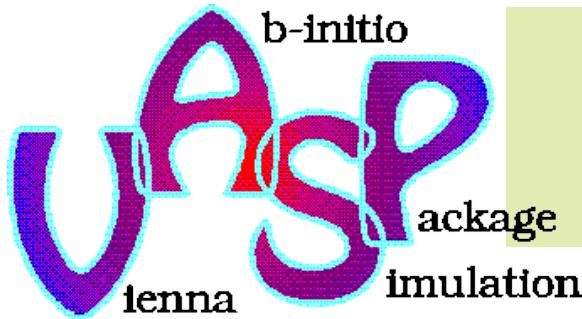
- Simple geometry arguments based on a critical ionic (Shannon radii) **fail**, high Ba ion polarizability and the **electronic structure** are important factors.
- 3 key factors determining migration barrier through A-A'-B triangle are:
- Displacements of A-type ions from jumping O\*
- Displacement (tilting) of a whole BO<sub>4</sub>O\*
- Covalency of B-O\* chemical bond
- clear correlation between oxygen migration and vacancy formation energies

# Thank you for your attention!

- **2. Quantum chemical approach**
- **CRYSTAL 2014** code with LCAO basis set
- (re-optimised Comp Mat Sci. 29, 165 (2004))

For light atoms (O), all-electron basis set (BS) for heavy atoms (Sr, Pb,Ti and Zr), the **small-core pseudopotentials**

- **Hybrid HF-DFT functionals** work very good for band gaps
- Bond populations and atomic charge analysis
- Well suited for slabs
- **Ghost basis set on vacant sites**



# Methods: 1. Solid state physics

## Density Functional Theory Plane Wave basis set

**Generalised Gradient Approximation (Hubbard U)**

**GGA, GGA+U, PBE0 hybrid** exchange-correlation functional

**Projector Augmented Wave** method

**Conjugate Gradient** method for structure relaxation

**Nudged Elastic Bands** for energy barriers estimation

**Bader charge** analysis

**Spin-polarized calculations**

# Factors determining O diffusion?

